Hanoi attractors and the Sierpiński gasket: Geometric and analytic convergence

Patricia Alonso-Ruiz

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For each $\alpha \in (0, 1/3)$, we define the so-called Hanoi attractor K_{α} . We show that the sequence $(K_{\alpha})_{\alpha}$ converges to the Sierpiński gasket K with respect to the Hausdorff metric as α tends to 0, and the Hausdorff dimension converges too. In view of this result, we look for an analytic convergence: We define a Laplacian on K_{α} , whose asymptotic behaviour will be studied and compared with the one corresponding to K. Since K_{α} is not self-similar, we will have to modify the classical construction of the Laplace operator for p.c.f. self-similar fractals by Kigami, Strichartz et al.